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DATE

# Square And Square roots, cube and cube roots

## Exercise 3-A

Ques-1 Find the square of each of the following numbers:-

i) 14

$$14^2 = 14 \times 14 \\ = 196$$

ii) 137

$$137^2 = 137 \times 137 \\ = 18769$$

iii)  $\frac{4}{17}$

$$\left[\frac{4}{17}\right]^2 = \frac{4 \times 4}{17 \times 17} = \frac{16}{289}$$

iv)  $2\frac{3}{4}$

$$\cancel{2} + \frac{2 \times 4 + 3}{4} = \frac{8 + 3}{4} = \frac{11}{4}$$

$$\left[\frac{11}{4}\right]^2 = \frac{11 \times 11}{4 \times 4} = \frac{121}{16} = 7\frac{9}{16}$$

v) 0.01

$$0.01 = \frac{1}{100}$$

$$\left[ \frac{1}{100} \right]^2 = \frac{1 \times 1}{100 \times 100} = \frac{1}{10000} = 0.0001$$

vi) 1.2

$$1.2 = \frac{12}{10}$$

$$\left[ \frac{12}{10} \right]^2 = \frac{12 \times 12}{10 \times 10} = \frac{144}{100} = 1.44$$

vii) 0.17

~~0.17~~ 0.17 =  $\frac{17}{100}$

$$\left[ \frac{17}{100} \right]^2 = \frac{17 \times 17}{100 \times 100} = \frac{289}{10000} = 0.0289$$

viii) 4.6

$$4.6 = \frac{46}{10}$$

$$\left[ \frac{46}{10} \right]^2 = \frac{46 \times 46}{10 \times 10} = \frac{2116}{100} = 21.16$$

Ques-2 using Prime factorization method, find which of the following are perfect square numbers:-

i) 252

$$\begin{array}{r} 2 \overline{) 252} \\ \underline{4} \phantom{00} \\ 210 \phantom{0} \\ \underline{420} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 126} \\ \underline{252} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 63} \\ \underline{126} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 21} \\ \underline{42} \\ 0 \end{array}$$

$$\begin{array}{r} 7 \overline{) 7} \\ \underline{14} \\ 0 \end{array}$$

1

$$252 = \overline{2 \times 2} \times \overline{3 \times 3} \times 7$$

$\therefore$  252 is not a perfect square

ii) 324

$$\begin{array}{r} 2 \overline{) 324} \\ \underline{648} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 162} \\ \underline{324} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 81} \\ \underline{162} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 27} \\ \underline{54} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 9} \\ \underline{18} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{) 3} \\ \underline{6} \\ 0 \end{array}$$

1

$$324 = \overline{2 \times 2} \times \overline{3 \times 3} \times \overline{3 \times 3}$$

$\therefore$  324 is a perfect square number

iii) 676

$$\begin{array}{r} 2 \overline{) 676} \\ \underline{1352} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 338} \\ \underline{676} \\ 0 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 676} \\
 \underline{2 \ 338} \\
 13 \ 169 \\
 \underline{13 \ 13} \\
 1
 \end{array}$$

$$676 = \overline{2 \times 2} \times \overline{13 \times 13}$$

$\therefore 676$  is a perfect square number.

iv) 1225

$$\begin{array}{r}
 5 \overline{) 1225} \\
 \underline{5 \ 245} \\
 7 \ 49 \\
 \underline{7 \ 7} \\
 1
 \end{array}$$

$$1225 = \overline{5 \times 5} \times \overline{7 \times 7}$$

$\therefore 1225$  is a perfect square number.

v) 2916

$$\begin{array}{r}
 2 \overline{) 2916} \\
 \underline{2 \ 1458} \\
 3 \ 729 \\
 \underline{3 \ 438} \\
 3 \ 81 \\
 \underline{3 \ 27} \\
 3 \ 9 \\
 \underline{3 \ 3} \\
 1
 \end{array}$$

$$2916 = \overline{2 \times 2} \times \overline{3 \times 3} \times \overline{3 \times 3} \times \overline{3 \times 3} \times \overline{3}$$

$\therefore 2916$  is a perfect square number.

vi.) 3528

$$\begin{array}{r}
 2 \overline{) 3528} \\
 \underline{2} \phantom{0} \phantom{0} \phantom{0} \\
 1764 \\
 \underline{2} \phantom{0} \phantom{0} \phantom{0} \\
 882 \\
 \underline{3} \phantom{0} \phantom{0} \phantom{0} \\
 441 \\
 \underline{3} \phantom{0} \phantom{0} \phantom{0} \\
 147 \\
 \underline{7} \phantom{0} \phantom{0} \phantom{0} \\
 49 \\
 \underline{7} \phantom{0} \phantom{0} \phantom{0} \\
 7 \\
 \underline{1} \\
 1
 \end{array}$$

$3528 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$   
 $\therefore 3528$  is a perfect square number.

vii.) 5625

$$\begin{array}{r}
 3 \overline{) 5625} \\
 \underline{3} \phantom{0} \phantom{0} \phantom{0} \\
 1875 \\
 \underline{5} \phantom{0} \phantom{0} \phantom{0} \\
 625 \\
 \underline{5} \phantom{0} \phantom{0} \phantom{0} \\
 125 \\
 \underline{5} \phantom{0} \phantom{0} \phantom{0} \\
 25 \\
 \underline{5} \phantom{0} \phantom{0} \phantom{0} \\
 5 \\
 \underline{1} \\
 1
 \end{array}$$

$5625 = 3 \times 3 \times 5 \times 5 \times 5 \times 5$   
 $\therefore 5625$  is a perfect square number.

viii.) 9075

$$\begin{array}{r}
 3 \overline{) 9075} \\
 \underline{3} \phantom{0} \phantom{0} \phantom{0} \\
 3025 \\
 \underline{5} \phantom{0} \phantom{0} \phantom{0} \\
 605 \\
 \underline{11} \phantom{0} \phantom{0} \phantom{0} \\
 121 \\
 \underline{11} \phantom{0} \phantom{0} \phantom{0} \\
 11
 \end{array}$$

$$9075 = 3 \times 5 \times 5 \times 11 \times 11$$

$\therefore 9075$  is a perfect square number.

Ques 3 Show that each of the following numbers is a perfect square. Also, find their square roots.

i) 441

$$\begin{array}{r} 3 \overline{)441} \\ \underline{3147} \\ 749 \\ \underline{747} \\ 1 \end{array}$$

$$441 = 3 \times 3 \times 7 \times 7$$

$\therefore 441$  is a perfect square number.

$$441 = 3 \times 3 \times 7 \times 7$$

$$\sqrt{441} = 3 \times 7 = 21$$

ii.) 784

$$\begin{array}{r} 2 \overline{)784} \\ \underline{2392} \\ 2196 \\ \underline{2198} \\ 749 \\ \underline{747} \\ 1 \end{array}$$

$$784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$$

$\therefore 784$  is a perfect square number.

$$9075 = 3 \times 5 \times 5 \times 11 \times 11$$

$\therefore 9075$  is a perfect square number.

Ans 3 Show that each of the following numbers is a perfect square. Also, find the square root of each:-

i) 441

$$\begin{array}{r} 3 \overline{)441} \\ \underline{3} \phant{0} \phant{0} \\ 147 \\ \underline{147} \\ 0 \phant{0} \phant{0} \\ 7 \overline{)49} \\ \underline{7} \phant{0} \\ 7 \\ \underline{7} \\ 0 \phant{0} \\ 1 \end{array}$$

$$441 = 3 \times 3 \times 7 \times 7$$

$\therefore 441$  is a perfect square number.

$$\begin{aligned} 441 &= 3 \times 3 \times 7 \times 7 \\ \sqrt{441} &= 3 \times 7 = 21 \end{aligned}$$

ii) 784

$$\begin{array}{r} 2 \overline{)784} \\ \underline{2} \phant{0} \phant{0} \\ 392 \\ \underline{392} \\ 0 \phant{0} \phant{0} \\ 2 \overline{)196} \\ \underline{2} \phant{0} \phant{0} \\ 98 \\ \underline{98} \\ 0 \phant{0} \phant{0} \\ 7 \overline{)49} \\ \underline{7} \phant{0} \\ 7 \\ \underline{7} \\ 0 \phant{0} \\ 1 \end{array}$$

$$784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$$

$\therefore 784$  is a perfect square number.

$$784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$$

$$\sqrt{784} = 2 \times 2 \times 7 = 4 \times 7 = 28$$

(ii) 1225

$$5 \overline{) 1225}$$

$$5 \overline{) 245}$$

$$7 \overline{) 49}$$

$$7 \overline{) 7}$$

1

$$1225 = \overline{5 \times 5} \times \overline{7 \times 7}$$

$\therefore$  1225 is a perfect square number

$$1225 = 2 \cdot 5 \times 5 \times 7 \times 7$$

$$\sqrt{1225} = 5 \times 7 = 35$$

(iv) 3969

$$3 \overline{) 3969}$$

$$3 \overline{) 1323}$$

$$3 \overline{) 441}$$

$$3 \overline{) 147}$$

$$7 \overline{) 49}$$

$$7 \overline{) 7}$$

1

$$3969 = \overline{3 \times 3} \times \overline{3 \times 3} \times \overline{7 \times 7}$$

$\therefore$  3969 is a perfect square number

$$3969 = 3 \times 3 \times 3 \times 3 \times 7 \times 7$$

$$\sqrt{3969} = 3 \times 3 \times 7 = 9 \times 7 = 63$$



v.) 2601

$$\begin{array}{r} 3 \overline{)2601} \\ \underline{3 \ 867} \\ 17 \overline{)289} \\ \underline{17 \ 117} \\ 1 \end{array}$$

$$2601 = \overline{3 \times 3} \times \overline{17 \times 17}$$

$\therefore$  2601 is a perfect square number

$$2601 = 3 \times 3 \times 17 \times 17$$

$$\sqrt{2601} = 3 \times 17 = 51$$

vi.) 5929

$$\begin{array}{r} 11 \overline{)5929} \\ \underline{11 \ 539} \\ 7 \overline{)749} \\ \underline{7 \ 7} \\ 1 \end{array}$$

$$5929 = \overline{11 \times 11} \times \overline{7 \times 7}$$

$\therefore$  5929 is a perfect square number

$$5929 = \overline{11 \times 11} \times \overline{7 \times 7}$$

$$\sqrt{5929} = 11 \times 7 = 77$$

vii.) 7056

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$$\begin{array}{r} 2 \overline{)7056} \\ \underline{2 \ 3528} \\ 2 \overline{)3528} \\ \underline{2 \ 1764} \\ 3 \overline{)1764} \\ \underline{3 \ 1447} \\ 2 \overline{)1447} \\ \underline{2 \ 49} \\ 7 \overline{)49} \\ \underline{7 \ 7} \\ 1 \end{array}$$

$$7056 = \overline{2 \times 2 \times 2 \times 2} \times \overline{3 \times 3 \times 3 \times 3} \times \overline{7 \times 7}$$

$\therefore 7056$  is a perfect square number

$$7056 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 7 \times 7$$

$$\sqrt{7056} = \cancel{2 \times 2 \times 3 \times 3 \times 7} = \cancel{4 \times 3 \times 3 \times 7} = \cancel{12 \times 3 \times 7} = \frac{36}{\cancel{12}} \times 7 =$$

$$\sqrt{7056} = 2 \times 2 \times 3 \times 3 \times 7 = 252$$

viii.) 8281

$$\begin{array}{r} 7 \overline{) 8281} \\ 7 \overline{) 1183} \\ 13 \overline{) 169} \\ 13 \overline{) 13} \\ 1 \end{array}$$

$$8281 = \overline{7 \times 7} \times \overline{13 \times 13}$$

$\therefore 8281$  is a perfect square number

$$8281 = 7 \times 7 \times 13 \times 13$$

$$\sqrt{8281} = 7 \times 13 = 91$$

Ques 4 Find the smallest number by which each of the following numbers must be multiplied to get a perfect square number. Also, find the square root of the resulting number.

i) 588

$$588 = \overline{2 \times 2} \times \textcircled{3} \times \overline{7 \times 7}$$

So we multiply by 3

$$\begin{array}{r} 2 \overline{) 588} \\ 2 \overline{) 294} \\ 3 \overline{) 147} \\ 7 \overline{) 49} \\ 7 \overline{) 7} \\ 1 \end{array}$$

Perfect square number =  $58813$   
 $= 1764$   
 $= 2 \times 2 \times 3 \times 3 \times 7 \times 7$

$$\sqrt{1764} = 2 \times 3 \times 7$$

$$= 42$$

ii) 2592

$\begin{array}{r} 2 \overline{) 2592} \\ 2 \overline{) 1296} \\ 2 \overline{) 648} \\ 2 \overline{) 324} \\ 2 \overline{) 162} \\ 3 \overline{) 81} \\ 3 \overline{) 27} \\ 3 \overline{) 9} \\ 3 \overline{) 3} \\ 1 \end{array}$	$2592 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$ So, we multiply by 2 Perfect square number = $2592 \times 2 = 5184$ $= 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$ $\sqrt{5184} = 2 \times 2 \times 2 \times 3 \times 3$ $= 72$
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iii) 3332

$3332 = 2 \times 2 \times 7 \times 17 \times 17$   
 So, we multiply by 17

$\begin{array}{r} 2 \overline{) 3332} \\ 2 \overline{) 1666} \\ 7 \overline{) 833} \\ 17 \overline{) 119} \\ 17 \overline{) 17} \\ 1 \end{array}$
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Perfect square number =  $3332 \times 17$   
 $= 56644$

$$= 2 \times 2 \times 7 \times 17 \times 17 \times 17 \times 17$$

$$\sqrt{56644} = 2 \times 7 \times 17 = 238$$

iv) 3380

$$3380 = 2 \times 2 \times 5 \times 13 \times 13$$

So, we multiply by 5

$$\text{Perfect square number} = 3380 \times 5 = 16900$$

$$= 2 \times 2 \times 5 \times 5 \times 13 \times 13$$

$$\sqrt{16900} = 2 \times 5 \times 13 = 130$$

$$\begin{array}{r} 2 \overline{) 3380} \\ 2 \overline{) 1690} \\ 5 \overline{) 845} \\ 13 \overline{) 69} \\ 13 \overline{) 13} \\ 1 \end{array}$$

Ques-5 By which least number should the given number be divided to obtain a perfect square number? Also, find the resulting perfect square number and its square roots.

i) 1728  $\rightarrow$

$$1728 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3$$

So, we divide by 3

$$\begin{aligned} \text{Perfect square number} &= 1728 \div 3 \\ &= 576 \end{aligned}$$

$$576 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$$

$$\begin{aligned} \sqrt{576} &= 2 \times 2 \times 2 \times 3 \\ &= 24 \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 1728} \\ 2 \overline{) 864} \\ 2 \overline{) 432} \\ 2 \overline{) 216} \\ 2 \overline{) 108} \\ 2 \overline{) 54} \\ 3 \overline{) 27} \\ 3 \overline{) 9} \\ 3 \overline{) 3} \\ 1 \end{array}$$

ii) 4500  $\rightarrow$

$$4500 = 2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 5$$

So, we divided by 5

Perfect square number =  $4500 \div 5$   
 $= 900$

$900 = 2 \times 2 \times 3 \times 3 \times 5 \times 5$

$\sqrt{900} = 2 \times 3 \times 5 = 30$

iii) 7776  $\rightarrow$

$7776 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3$   
 $= 2 \times 3 = 6$

So, we divided by 6

Perfect square number =  $7776 \div 6$   
 $= 1296$

$1296 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$

$\sqrt{1296} = 2 \times 2 \times 3 \times 3 = 36$

2	7776
2	3888
2	1944
2	972
2	486
3	243
3	81
3	27
3	9
3	3
	1

iv) 8820

$8820 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$

So, we divided it by 5

Perfect square number =  $8820 \div 5$   
 $= 1764$

$1764 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$

$\sqrt{1764} = 2 \times 3 \times 7 = 42$

2	8820
2	4410
3	2205
3	735
5	245
7	49
7	7
	1

Ques-6 The students of a class arranged a picnic. Each student contributed as many rupees as the

number of students in the class. If the total contribution is ₹1156, find the strength of the class?

Let no. of students be  $x$   
Rs given by each student be  $x$

$$\begin{aligned} \text{Total amount} &= x \times x \\ &= x^2 \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 1156} \\ \underline{4} \phantom{00} \\ 278 \\ \underline{556} \\ 200 \\ \underline{1700} \\ 300 \\ \underline{1700} \\ 300 \\ \underline{1700} \\ 300 \\ \underline{1700} \\ 300 \end{array}$$

According to Question

$$\begin{aligned} x^2 &= 1156 \\ x &= \sqrt{1156} \\ x &= \sqrt{2 \times 2 \times 17 \times 17} \\ &= 2 \times 17 = 34 \end{aligned}$$

Ques-7 In an auditorium, the number of rows is equal to the number of chairs in each row. If the capacity of the auditorium is 2025, find the number of chairs in each row?

Let no. of rows be  $x$   
Number of chairs in each row be  $x$

$$\begin{aligned} \text{Total Capacity} &= x \times x \\ &= x^2 \end{aligned}$$

$$\begin{array}{r} 3 \overline{) 2025} \\ \underline{6} \phantom{00} \\ 2025 \\ \underline{6075} \\ 1425 \\ \underline{1350} \\ 75 \\ \underline{75} \\ 0 \end{array}$$

According to Question

$$\begin{aligned} x^2 &= 2025 \\ x &= \sqrt{2025} \\ x &= \sqrt{3 \times 3 \times 3 \times 3 \times 5 \times 5} \\ x &= 3 \times 3 \times 5 = 45 \end{aligned}$$

Q-8 Find the least square number which is exactly divisible by each of the numbers 8, 9, 10 and 15.

$$2 \mid 8, 9, 10, 15$$

$$2 \mid 4, 9, 5, 15$$

$$2 \mid 2, 9, 5, 15$$

$$3 \mid 1, 9, 5, 15$$

$$3 \mid 1, 3, 5, 5$$

$$5 \mid 1, 1, 5, 5$$

$$1, 1, 1, 1$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 \times 3 \times 5$$

$$= 360$$

$$2 \mid 240$$

$$2 \mid 120$$

$$2 \mid 60$$

$$2 \mid 30$$

$$3 \mid 15$$

$$5 \mid 5$$

$$1$$

$$240 = \overline{2 \times 2} \times \overline{2} \times \overline{3} \times \overline{3} \times \overline{5}$$

$$= 2 \times 5 = 10$$

To make it a perfect square number, it must be multiplied by  $2 \times 5$ , i.e., by 10

Hence the required number =  $360 \times 10 = 3600$

## Square and Square roots, Cube and Cube roots

### Properties of a Perfect square -

- I) The square of an even number is always an even number.
- II) The square of an odd number is always an odd number.
- III) The square of a proper fraction is a proper fraction less than the given fraction.
- IV) The square of a decimal fraction less than 1 is smaller than the given decimal.
- V) A number ending in 2, 3, 7 or 8 is never a perfect square.
- VI) A number ending in an odd number of zeros is never a perfect square.

### Interesting Patterns in squares of Numbers

I) Pythagorean Triplets - For every natural number  $m > 1$ , we have  $(2m, m^2 - 1, m^2 + 1)$  as a Pythagorean triplet.

II) Between two consecutive square numbers  $n^2$  and  $(n+1)^2$ , there are  $2n$  non-perfect square numbers.

III) using the identity  $(a+b)^2 = (a^2 + 2ab + b^2)$  to



evaluate square of numbers.

IV) using the identity  $(a-b)^2 = (a^2 - 2ab + b^2)$  to evaluate squares of numbers.

V) using the identity  $(a-b)(a+b) = a^2 - b^2$  to find the product of two consecutive odd or two consecutive even numbers.

### Exercise 3-B

Ques 1 Give reason to show that none of the numbers is a perfect square -

i) 2162

2162 is not a perfect square because a number ending 2, 3, 7 or 8 is never a perfect square.

ii) 6843

6843 is not a perfect square because a number ending 2, 3, 7 or 8 is never a perfect square.

iii) 9637

9637 is not a perfect square because a number ending 2, 3, 7 or 8 is never a perfect square.

iii) 6543

6543 is not a perfect square because a number ending 2, 3, 7 or 8 is never a perfect square.

iv) 640

640 is not a perfect square because a number ending in an odd number of zeros is never a perfect square.

v) 49000

49000 is not a perfect square because a number ending in an odd number of zeros is never a perfect square.

vii) 3600000

3600000 is not a perfect square because a number ending in an odd number of zeros is never a perfect square.

Ques 2) which of the following are squares of even numbers?

- i) 676    ii) 729    iii) 1089    iv) 2304    v) 5625  
vi) 9216

The square of an even number is always an even number.

676, 2304 and 9216 are squares of even numbers.

Ques 3 Which of the following are squares of odd numbers?

- i) 484      ii) 961      iii) 4225      iv) 7396
- v) 6241      vi) 8649

The square of an odd number is always an odd number.  
 961, 4225, 8649 are squares of odd numbers.

Ques 4 Without adding find the sum:-

i)  $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21$   
 $= (11)^2 = 11 \times 11 = 121$

ii)  $1 + 3 + 5 + 7 + \dots + 47 + 49$   
 $= (25)^2 = 25 \times 25 = 625$

iii)  $1 + 3 + 5 + 7 + \dots + 97 + 99$   
 $= (50)^2 = 50 \times 50 = 2500$

Ques-5 i) Express 144 as the sum of 12 odd numbers

$$144 = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23$$

ii) Express 225 as the sum of 15 odd numbers

$$225 = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23 + 25 + 27 + 29$$

Q.6 write a pythagorean triplet whose smallest number is -

i) 6  
Pythagorean triplets are  $= 2n, n^2-1, n^2+1$

$$2n = 6 = \frac{6}{2} = 3$$

$$n = 3$$

$$\begin{aligned} \text{Pythagorean triplets are} &= 2 \times 3, 3^2-1, 3^2+1 \\ &= 6, 9-1, 9+1 \\ &= 6, 8, 10 \end{aligned}$$

ii) 14  
Pythagorean triplets are  $= 2n, n^2-1, n^2+1$

$$2n = 14 = \frac{14}{2} = 7$$

$$n = 7$$

$$\begin{aligned} \text{Pythagorean triplets are} &= 2 \times 7, 7^2-1, 7^2+1 \\ &= 14, 49-1, 49+1 \\ &= 14, 48, 50 \end{aligned}$$

ii) 16  
Pythagorean triplets are  $= 2n, n^2-1, n^2+1$

$$2n = 16 = \frac{16}{2} = 8 \Rightarrow n = 8$$

$$\begin{aligned} \text{Pythagorean triplets are} &= 2 \times 8, 8^2-1, 8^2+1 \\ &= 16, 64-1, 64+1 \\ &= 16, 63, 65 \end{aligned}$$

iv) 20

Pythagorean triplets are  $= 2n, n^2-1, n^2+1$ 

$$2n = 20 = 2 \times 10 = 10$$

Pythagorean triplets are  $= 2 \times 10, 10^2-1, 10^2+1$   
 $= 20, 100-1, 100+1$   
 $= 20, 99, 101$

Q.7 Evaluate :-

i)  $(29)^2 - (28)^2$

$$(n+1)^2 - n^2 = (n+1) + n$$

$$(29)^2 - (28)^2 = 29 + 28$$

$$= 57$$

ii)  $(56)^2 - (55)^2$

$$(n+1)^2 - n^2 = (n+1) + n$$

$$(56)^2 - (55)^2 = 56 + 55$$

$$= 111$$

iii)  $(82)^2 - (81)^2$

$$(n+1)^2 - n^2 = (n+1) + n$$

$$(82)^2 - (81)^2 = 82 + 81$$

$$= 163$$

iv)  $(108)^2 - (107)^2$

$$(n+1)^2 - n^2 = (n+1) + n$$

$$(108)^2 - (107)^2 = 108 + 107 = 215$$

$$v.) (221)^2 - (220)^2$$

$$(n+1)^2 - n^2 = (n+1) + n$$

$$(221)^2 - (220)^2 = 221 + 220 \\ = 441$$

Q-8 using the identity  $(a+b)^2 = (a^2 + 2ab + b^2)$ ,  
evaluate :-

i)  $(204)^2$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(204)^2 = (200+4)^2$$

$$= (200)^2 + 2 \times 200 \times 4 + 4^2$$

$$= 40000 + 1600 + 16$$

$$= 41616$$

ii)  $(307)^2$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(307)^2 = (300+7)^2$$

$$= (300)^2 + 2 \times 300 \times 7 + 7^2$$

$$= 90000 + 4200 + 49$$

$$= 94249$$

iii)  $(430)^2$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(430)^2 = (400+30)^2$$

$$= (400)^2 + 2 \times 400 \times 30 + 30^2$$

$$= 160000 + 24000 + 900$$

$$= 184900$$

Q-9 using the identity  $(a-b)^2 = (a^2 - 2ab + b^2)$ , evaluate:

i)  $(94)^2$

$$(a-b)^2 = (a^2 - 2ab + b^2)$$

$$\begin{aligned}(94)^2 &= (100-6)^2 \\ &= 100^2 - 2 \times 100 \times 6 + 6^2 \\ &= 10000 - 1200 + 36 \\ &= 10036 - 1200 \\ &= 8836\end{aligned}$$

ii)  $(192)^2$

$$(a-b)^2 = (a^2 - 2ab + b^2)$$

$$\begin{aligned}(192)^2 &= (200-8)^2 \\ &= 200^2 - 2 \times 200 \times 8 + 8^2 \\ &= 40000 - 3200 + 64 \\ &= 40064 - 3200 \\ &= 36864\end{aligned}$$

iii)  $(389)^2$

$$(a-b)^2 = (a^2 - 2ab + b^2)$$

$$\begin{aligned}(389)^2 &= (400-11)^2 \\ &= 400^2 - 2 \times 400 \times 11 + 11^2 \\ &= 160000 - 8800 + 121 \\ &= 160121 - 8800 \\ &= 151321\end{aligned}$$

Evaluate:-

8.10

i)  $59 \times 61$

$$(a-b)(a+b) = a^2 - b^2$$

$$= (60-1) \times (60+1)$$

$$= 60^2 - 1^2$$

$$= 3600 - 1$$

$$= 3599$$

ii)  $88 \times 92$

$$(a-b)(a+b) = a^2 - b^2$$

$$= (90-2) \times (90+2)$$

$$= 90^2 - 2^2$$

$$= 8100 - 4$$

$$= 8096$$

iii)  $94 \times 106$

$$(a-b)(a+b) = a^2 - b^2$$

$$= (100-6) \times (100+6)$$

$$= 100^2 - 6^2$$

$$= 10000 - 36$$

$$= 10964$$

iv)  $48 \times 52$

$$(a-b)(a+b) = a^2 - b^2$$



$$(50-2)(50+2)$$

$$= 50^2 - 2^2$$

$$= 2500 - 4$$

$$= 2496$$

Q-11 State whether each of the following statements is true or false:-

i) A perfect square number always has an even number of digits.

False

ii) Every number ending in an even number of zeros is a perfect square.

ii) False

iii) The square of a prime number is prime.

iii) False

iv) There are 10 perfect squares ~~is a perfect square~~ numbers from 1 to 100.

iv) True

v) The sum of two perfect squares is a perfect square.

False

vi) The difference of two perfect squares is a perfect square. False

vii) The product of two perfect squares is a perfect square. True

## Exercise 3-C

1) Find the square root of each of the following numbers by using division method -

i) 576

$$\begin{array}{r} 2 \overline{) 576} \quad (24 \\ \underline{4} \phantom{00} \\ 176 \\ \underline{-176} \\ \phantom{000} \\ \phantom{000} \\ \phantom{000} \end{array}$$

$$\sqrt{576} = 24$$

ii) 961

$$\begin{array}{r} 3 \overline{) 961} \quad (31 \\ \underline{9} \phantom{00} \\ \phantom{00} 61 \\ \underline{-61} \\ \phantom{000} \\ \phantom{000} \\ \phantom{000} \end{array}$$

$$\sqrt{961} = 31$$

iii) 1444

$$\begin{array}{r} 3 \overline{) 1444} \quad (38 \\ \underline{9} \phantom{00} \\ \phantom{00} 544 \\ \underline{-544} \\ \phantom{000} \\ \phantom{000} \\ \phantom{000} \end{array}$$

$$\sqrt{1444} = 38$$

iv) 4489

$$\begin{array}{r|l}
 6 & \overline{44} \quad \overline{89} \quad (67) \\
 6 & 36 \quad \downarrow \downarrow \\
 67 & \times 889 \\
 & \underline{- 889} \\
 & \quad \times \times \times
 \end{array}$$

$$\sqrt{4489} = 67$$

v) 6241

$$\begin{array}{r|l}
 7 & \overline{62} \quad \overline{41} \quad (79) \\
 7 & 49 \quad \downarrow \downarrow \\
 79 & \cdot 1341 \\
 & \underline{- 1341} \\
 & \quad \times \times \times
 \end{array}$$

$$\sqrt{6241} = 79$$

vi) 5476

$$\begin{array}{r|l}
 7 & \overline{54} \quad \overline{76} \quad (74) \\
 7 & 49 \quad \downarrow \downarrow \\
 74 & \quad 576 \\
 & \underline{- 576} \\
 & \quad \times \times \times
 \end{array}$$

$$\sqrt{5476} = 74$$

vii) 9025

$$\begin{array}{r}
 95 \ 25 \quad (95) \\
 95 \ 25 \\
 \underline{95 \ 25} \\
 0000 \\
 \times \times \times
 \end{array}$$

$$\sqrt{9025} = 95$$

$$\begin{array}{r}
 87 \\
 8 \ 75 \ 69 \quad )87 \\
 \underline{8 \ 75} \ 69 \\
 8 \ 75 \ 69 \\
 \underline{8 \ 75 \ 69} \\
 0000 \\
 \times \times \times
 \end{array}$$

$$\sqrt{7569} = 87$$

Ques 2 The area of a square field is 7744 sq. metres.  
Find its perimeter.

$$\text{Area of square} = \text{Side} \times \text{Side}$$

$$7744 \text{ sq. metres} = \text{Side} \times \text{Side}$$

$$\text{Side} = \sqrt{7744}$$

$$\begin{array}{r}
 88 \\
 8 \ 88 \ 44 \quad (88) \\
 \underline{8 \ 88} \ 44 \\
 8 \ 88 \ 44 \\
 \underline{8 \ 88 \ 44} \\
 0000 \\
 \times \times \times
 \end{array}$$

$$\sqrt{7744} = 88 = \text{Side of square is } 88 \text{ cm.}$$

Q-3 Find the least number which must be subtracted from 1104 to obtain a perfect square. Find this perfect square and its square root.

$$\begin{array}{r}
 3 \quad \overline{) 1104} \quad (33 \\
 \underline{-9} \quad \downarrow \\
 63 \quad \underline{204} \\
 \underline{-189} \\
 \times 15
 \end{array}$$

Remainder = 15  
 $\therefore$  No. Subtracted = 15

Perfect square number =  $1104 - 15$   
 $= 1089$

$$\sqrt{1089} = 33$$

Q-4 Find the least number which must be ~~added~~ <sup>subtracted</sup> to ~~1104~~ <sup>1189</sup> to obtain a perfect square. Find this perfect square and its square root.

$$\begin{array}{r}
 8 \quad \overline{) 7956} \quad ( \\
 \underline{64} \quad \downarrow \\
 169 \quad \underline{1556} \\
 \underline{-1556} \\
 \times \times \times
 \end{array}$$

Remainder = 35  
 $\therefore$  Number Subtracted = 35

Perfect square number =  $7956 - 35$   
 $= 7921$

$$\sqrt{7921} = 89$$

Ques 5 Find the least number which must be added to 6203 to obtain a perfect square. Find the perfect square and its square root.

$$\begin{array}{r} 7 \quad \overline{62 \ 03} \ (78 \\ 7 \quad 49 \ \downarrow \\ 148 \quad 13 \ 03 \\ \quad \quad \underline{-11 \ 84} \\ \quad \quad \quad \underline{\times 119} \end{array}$$

$$78^2 < 6203 < 79^2$$

$$79^2 = 6241$$

$$\begin{aligned} \text{No. added} &= 6241 - 6203 \\ &= 38 \end{aligned}$$

Perfect square number = 6241

$$\sqrt{6241} = 79$$

Ques 6 Find the least number which must be added to 7348 to obtain a perfect square. Find the perfect square and its square root.

$$\begin{array}{r} 8 \quad \overline{73 \ 48} \ (85 \\ 8 \quad 64 \ \downarrow \\ 165 \quad \underline{\times 9 \ 48} \\ \quad \quad \underline{-948} \\ \quad \quad \quad \underline{\times \times \times} \end{array}$$

$$85^2 < 7348 < 86^2$$

$$86^2 = 7396$$

$$\text{Number added} = 7396 - 7348$$

$$= 48$$

Perfect square number = 7396

$$\sqrt{7396} = 86$$

Q-7 Find the greatest number of six digits which is a perfect square. Find the square root of this number.

Greatest number of six digits = 999999

Let us try to find the square root of 999999

9	99	99	99	) 999
9	-81	11	11	
184	899	11	11	
+ 4	-736	11	11	↓
<del>368</del>	16399	11	11	
1884	-14736	11	11	
				X 1663

clearly  $(994)^2$  is less than 999999 by 1663

So the least number to be subtracted is 1663

Hence, the required number

$$= 999999 - 1663 = 998336$$

Q.8 Find the least number of four digits which is a perfect square

Ans: Greatest Number of 3 digit = 999

$$\begin{array}{r} 3 \overline{) 999} \quad (31 \\ 3 \overline{) 9} \downarrow \downarrow \\ 61 \overline{) 99} \\ \underline{-61} \\ 38 \end{array}$$

$$31^2 < 999 < 32^2$$

$$\text{Required Number} = 32^2 = 1024$$

Q.9 Find the least number by which 691692 must be (i) decreased (ii) increased (iii) multiplied (iv) divided, to make it a perfect square.

$$\begin{array}{r} 2 \overline{) 691692} \quad (263 \\ 2 \overline{) 4} \downarrow \downarrow \\ 46 \overline{) 291} \\ 6 \overline{) 276} \\ 523 \overline{) 1592} \\ \underline{-1569} \\ \text{XX23} \end{array}$$

i) Number to be decreased = 23

$$\text{ii) } 263^2 < 69192 < 264^2$$

$$264^2 = 69696$$

$$69696 - 69192 = 508$$



Ques 8 Find the least number of four digits which is a perfect square

Ans 8 Greatest Number of 3 digit = 999

$$\begin{array}{r}
 3 \overline{)999} \text{ (31)} \\
 \underline{9} \quad \downarrow \\
 61 \overline{)99} \\
 \underline{61} \\
 38
 \end{array}$$

$$31^2 < 999 < 32^2$$

Required Number =  $32^2 = 1024$

Ques 9 Find the least number by which 691692 must be (i) decreased ii) increased & iii) multiplied iv) divided, to make it a perfect square.

$$\begin{array}{r}
 2 \overline{)691692} \text{ (263)} \\
 \underline{4} \quad \downarrow \\
 46 \overline{)291} \\
 \underline{6} \quad \downarrow \\
 523 \overline{)1592} \\
 \underline{1569} \\
 \text{XX23}
 \end{array}$$

i) Number to be decreased = 23

ii)  $263^2 < 69192 < 264^2$   
 $264^2 = 69696$

Number increased =  $69696 - 69192 = 508$

$$\begin{array}{r|l} \text{iii)} & 2 \ 69192 \\ & \underline{2 \ 84596} \\ & 2 \ 17298 \\ & \underline{3 \ 8649} \\ & 3 \ 2883 \\ & \underline{31 \ 961} \\ & 31 \ 31 \\ & \underline{\quad \quad 1} \end{array}$$

$$69192 = \sqrt{2 \times 2} \times 2 \times 3 \times 3 \times 31 \times 31$$

Number multiplied = 2

iv) No divided - 2